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## 3. Fachgespräch »Ortsbezogene Anwendungen und Dienste«

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# Modeling Context Constraints

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# Outline

Introduction

Context Model

Transformation of Context Dimensions

Service Scope Model

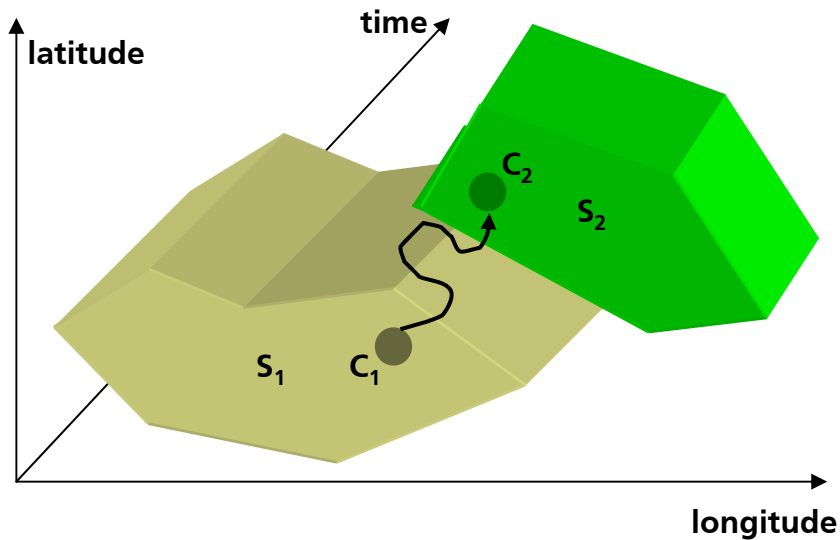
Service Scope Representation

Example

Conclusion



# Need for Defining Context Constraints: Service Roaming



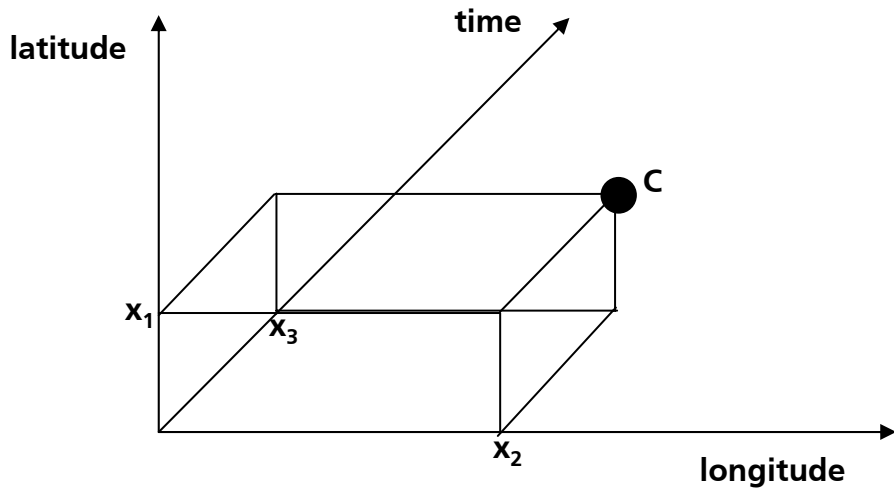
Services often have limited scope

Users (especially mobile users) change their contexts frequently

Services are valid for a certain user if user context is within service scope

Whenever the context leaves the scope service roaming is needed

# Context



Defined by values of  $n$  context dimensions

Represented by an  $n$ -tuple

In this example: 3 dimensions

$C = (\text{latitude}, \text{longitude}, \text{time})$

Certain value for each context dimension

Single point in context hyperspace

Current context values of an entity (a user)

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# Context Hyperspace

## Characteristics

Cartesian n-dimensional space

Dimensions defined for  $[-\infty; \infty]$

Dimensions defined on  $\mathbb{R}$

## Context attributes

Often limited range (e. g. longitude  $[-180;180]$ )

Not always defined on  $\mathbb{R}$  (e. g. room numbers)

Not always numbered (e. g. weather: cloudy)

Not always distinct (e. g. language capabilities: DE, EN)

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# Scales of Measurement, Scale of Representation

- Scales of measurement**
- Nominal  
Equal or unequal (e. g. male, female)
  - Ordinal  
Nominal + order of values (e. g. room numbers)
  - Interval  
Ordinal + definite difference (e. g. temperature)
  - Proportional / rational  
Interval + natural zero point (e. g. length)
- Scale of representation** - Always proportional scale (because defined on  $\mathbb{R}$ )

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# Transformation

## Context attributes

For each context attribute  $c_i$  there has to be a transformation into the representation attribute  $d_i$

$$\forall c_i : \exists f(c_i) \rightarrow d_i; d_i \in \mathbb{R}$$

This transformation is injective  
(For each input value there is a distinct output value)

## Context semantics

Context may consist of more than name/value pairs

Semantics are separated from values (semantic layer)

## Semantic layer

Contains scale of origin, relationships between context dimensions, ... (Not necessary for service roaming!)



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# Context Representation

## Operations

Proportional scale allows many operations  
(Order, difference, ratio, ...)

Only check for equality is needed for service roaming  
=> Only this is allowed on the context representation  
per default

All other operations are supported only if allowed by  
the semantic layer

## Integrity

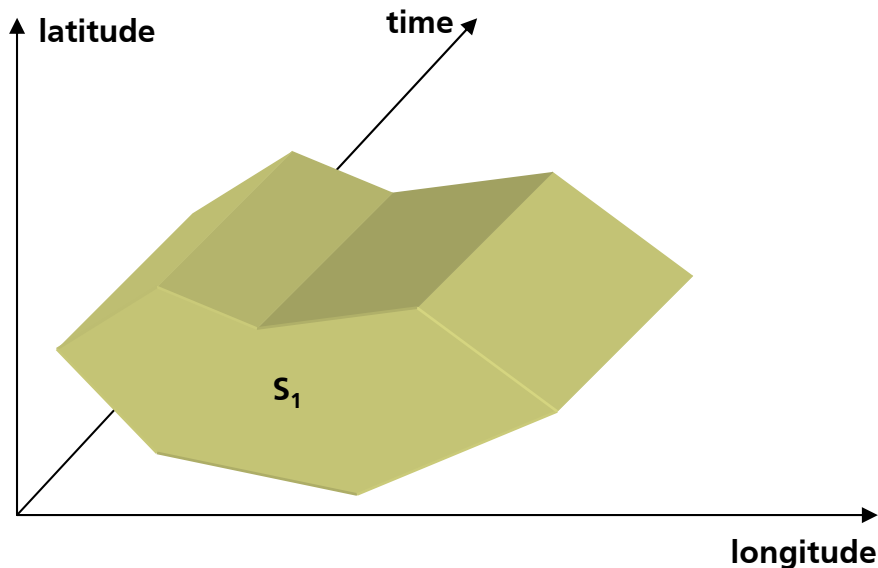
$$op(f(c_i)) = f(op(c_i))$$

**Reverse transformation** Leads to initial context value





# Service Scope Representation



Service scope: n-dimensional polytope  
(Assumption of linearity for simplification)

Two (popular) ways of representation:

- Boundary representation  
Each n-dimensional object is recursively described by its (n-1)-dimensional boundaries
- Constraint representation  
Systems of linear inequations, each of them defining a half-hyperspace

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# Comparison of Representations

## Boundary

Very popular in Solid Modeling

Used in GIS for representation of 2D/3D objects

Very verbose for n-dimensional objects (for large n's)

$$b_n \geq \prod_{i=1}^n i + 1 \quad (b_n: \text{number of bounding objects})$$

## Constraint

Only capable to describe convex objects

Less computation for ,INCLUDES' operator

Easier to convert boundary representation to constraint representation than other way round

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# Decision: Constraint Representation

## Reasons

Verbosity of boundary representation is major criteria

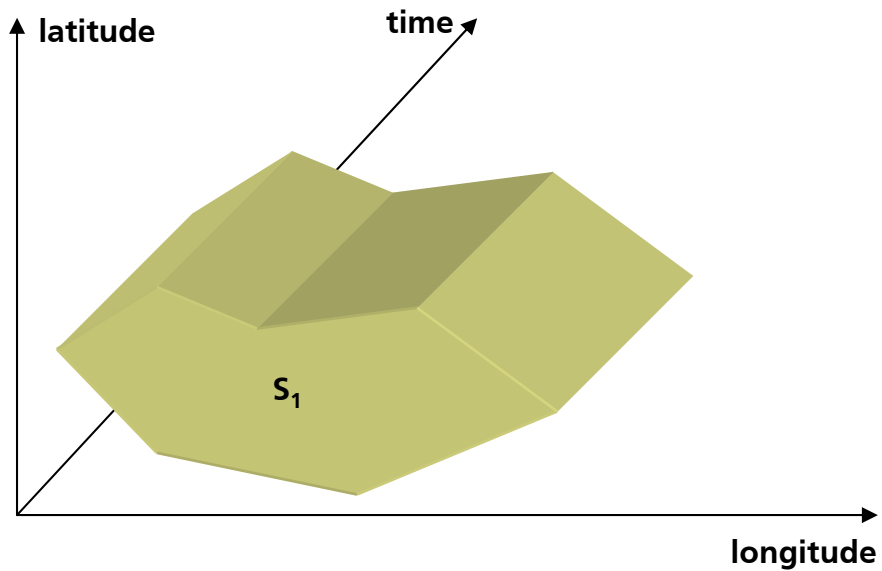
Many restrictions are already initially in constraint representation (e. g.  $\text{time} \geq 8:00$ )

Only few restrictions are initially in boundary representation (e. g. spatial restrictions by polygons)

## Non-convex scopes

Each non-convex polytope can be decomposed into a set of convex polytopes.

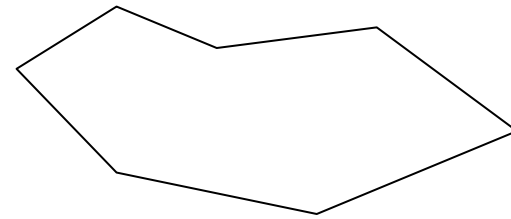
# Example



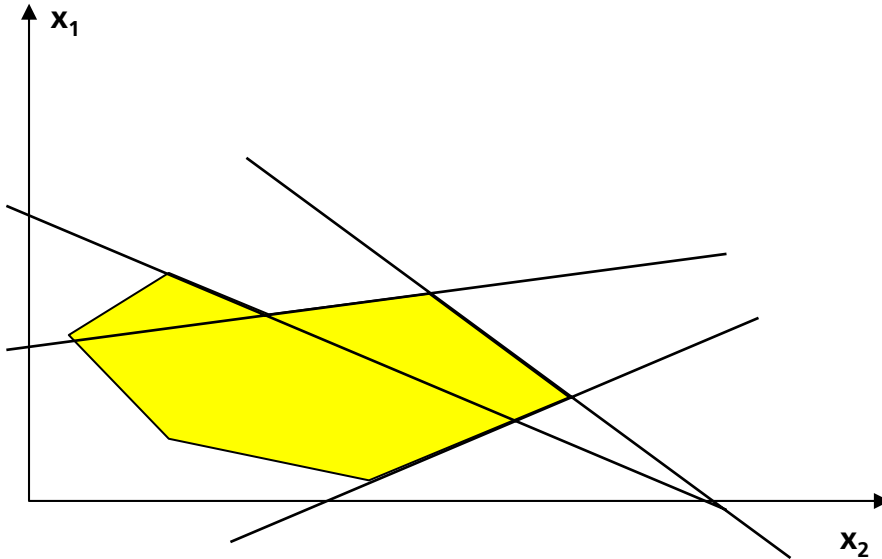
Constraints:

Time: between 8:00 and 21:00

Space: Within the following polygon



# Spatial Dimensions



1.  $x_1 = -x_2 + 1,4$
2.  $x_1 = -0,125x_2 + 0,6$
3.  $x_1 = 0,4x_2 - 0,9$
4.  $x_1 = -0,75x_2 + 3,6$
5.  $x_1 = 0,16x_2 + 1$
6.  $x_1 = -0,4x_2 + 2$
7.  $x_1 = 0,6x_2 + 1$

$$\begin{array}{lll}
 x_1 \geq -x_2 + 1,4 & \Leftrightarrow -x_1 - x_2 + 1,4 \leq 0 & (1) \\
 x_1 \geq -0,125x_2 + 0,6 & \Leftrightarrow -x_1 - 0,125x_2 + 0,6 \leq 0 & (2) \\
 x_1 \geq 0,4x_2 - 0,9 & \Leftrightarrow -x_1 + 0,4x_2 - 0,9 \leq 0 & (3) \\
 x_1 \leq -0,4x_2 + 2 & \Leftrightarrow x_1 + 0,4x_2 - 2 \leq 0 & (6) \\
 x_1 \leq 0,59x_2 + 1 & \Leftrightarrow x_1 - 0,59x_2 - 1 \leq 0 & (7)
 \end{array}$$

$$\begin{array}{lll}
 x_1 \geq 0,4x_2 - 0,9 & \Leftrightarrow -x_1 + 0,4x_2 - 0,9 \leq 0 & (3) \\
 x_1 \leq -0,75x_2 + 3,6 & \Leftrightarrow x_1 + 0,75x_2 - 3,6 \leq 0 & (4) \\
 x_1 \leq 0,16x_2 + 1 & \Leftrightarrow x_1 - 0,16x_2 - 1 \leq 0 & (5) \\
 x_1 \geq -0,4x_2 + 2 & \Leftrightarrow -x_1 - 0,4x_2 + 2 \leq 0 & (6)
 \end{array}$$

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# Time Dimension

## Restriction

Daily from 8:00 to 21:00

**Transformation daytime**  $d_{\text{time}} = f(c_{\text{time}}) = \text{hours}(c_{\text{time}}) * 60 + \text{minutes}(c_{\text{time}})$

$$c_{\text{time}} = 8:00 \Rightarrow d_{\text{time}} = 480$$

$$c_{\text{time}} = 21:00 \Rightarrow d_{\text{time}} = 1260$$

## Constraints

$$x_3 \geq 480 \quad \Leftrightarrow -x_3 + 480 \leq 0$$

$$x_3 \leq 1260 \quad \Leftrightarrow x_3 - 1260 \leq 0$$

# Matrix Representation of Service Scope

## Spatial Restrictions

$$-x_1 - x_2 + 1,4 \leq 0$$

$$-x_1 - 0,125x_2 + 0,6 \leq 0$$

$$-x_1 + 0,4x_2 - 0,9 \leq 0$$

$$x_1 + 0,4x_2 - 2 \leq 0$$

$$x_1 - 0,59x_2 - 1 \leq 0$$

$$-x_1 + 0,4x_2 - 0,9 \leq 0$$

$$x_1 + 0,75x_2 - 3,6 \leq 0$$

$$x_1 - 0,16x_2 - 1 \leq 0$$

$$-x_1 - 0,4x_2 + 2 \leq 0$$

## Time Restriction

$$-x_3 + 480 \leq 0$$

$$x_3 - 1260 \leq 0$$

## Matrices

$$\begin{pmatrix} -1 & -1 & 0 & 1,4 \\ -1 & -0,125 & 0 & 0,6 \\ -1 & 0,4 & 0 & -0,9 \\ 1 & 0,4 & 0 & -2 \\ 1 & -0,59 & 0 & -1 \\ 0 & 0 & -1 & 480 \\ 0 & 0 & 1 & -1260 \end{pmatrix} \vee \begin{pmatrix} -1 & 0,4 & 0 & -0,9 \\ 1 & 0,75 & 0 & -3,6 \\ 1 & -0,16 & 0 & -1 \\ -1 & -0,4 & 0 & 2 \\ 0 & 0 & -1 & 480 \\ 0 & 0 & 1 & -1260 \end{pmatrix}$$

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# Is Context Within Service Scope?

## Definition

Context is within service scope if context is element of the solution set of one of the matrices.

## Example

Context (2,9; 1,2; 555)  
(lat = 2,9; long = 1,2; time = 9:15)

## Result

$(2,9; 1,2; 555) \in \mathbb{L} (M_2)$

$\Rightarrow$  Context is within service scope and service is valid!



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# Conclusion

## Context model

Different context models exist in literature

Service roaming only needs context data

Context semantics are separated in semantic layer

Context data + semantic layer + transformation functions should maintain all information provided by existing context models

## Scope representation

Proposed representation is absolutely generic

Linear scopes should be sufficient

Constraint representation is preferable



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# Thanks for your attention!

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